

```

end;
shift := 0.0
end;
kon: a[n] := z;
n := n - 1
end of loop k
end of lager;

```

5. Examples

In general the accuracy of the algorithm is comparable with that of the QR algorithm. Convergence is very fast, three or four iterations per eigenvalue usually being adequate except for pathologically close eigenvalues. It should be stressed that the algorithm is expressly designed to find a comparatively low percentage of the largest or smallest eigenvalues; when a high percentage of eigenvalues is required the QR algorithm is to be preferred.

In order to illustrate that there is no significant loss of accuracy in the case of close eigenvalues, the results obtained with the matrices W_{21}^+ (Wilkinson, 1965) and $W_{21}^+ - 11I$ were computed on the CDC 3300 computer, using single precision floating-point binary computation with $t = 37$. W_{21}^+ is a symmetric tridiagonal matrix with

$$a_i = |11 - i|, \\ b_i = 1.$$

Some pairs of the eigenvalues are pathologically close. Merely for purpose of illustration all computed eigenvalues of both $W_{21}^+ - 11I$ and W_{21}^+ are given in Table 1 and Table 2 respectively. They are correct almost to working accuracy, though naturally since the matrices have eigenvalues which are equal to working accuracy the number of iterations is not typical.

References

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Table 1 Computed eigenvalues of $W_{21}^+ - 11I$

-0.2538	0582	2	-5.9997	5557	7
-0.2538	0582	3	-6.0002	1752	4
-1.7893	2135	6	-6.9956	4597	8
-1.7893	2135	7	-7.0039	5180	0
-2.9610	5888	1	-7.9569	0070	8
-2.9610	5888	8	-8.0389	4111	6
-3.9960	4779	3	-8.8697	9078	1
-3.9960	4820	4	-9.2106	7864	8
-4.9997	6597	1	-10.0524	6563	3
-4.9997	8248	0	-10.7461	9418	3
			-12.1254	4152	2

Table 2 Computed eigenvalues of W_{21}^+

10.7461	9417	7	5.0002	4442	3
10.7461	9417	6	4.9997	8247	6
9.2106	7864	3	4.0043	5402	2
9.2106	7864	2	3.9960	4820	0
8.0389	4111	9	3.0430	9929	2
8.0389	4111	2	2.9610	5888	3
7.0039	5220	7	2.1302	0921	9
7.0039	5179	6	1.7893	2135	2
6.0002	3402	9	0.9475	3436	7
6.0002	1752	0	0.2538	0581	7
			-1.1254	4152	2

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Eric Mutch Memorial

Eric Mutch, who, together with Harold Gearing, founded *The Computer Journal*, edited it for the first 12 years of its life, and created for it an international reputation for excellence, died in January 1969. The Publications Committee of The British Computer Society and the Editorial Board of the *Journal* wish to ensure that this excellent and far reaching work will be remembered.

To this end, the *Journal* is instituting a prize, to be offered at suitable intervals, to be known as the 'Eric Mutch Memorial' prize. The prize will have a value of £100 and will be awarded for the best paper to be submitted on a topic nominated by the Editorial Board.

Foremost among the objectives of the Board, when considering the topic to be chosen for the first competition, were the need to emphasise the role of the Society in bringing together the various disciplines involved in computing and the need to demonstrate to all members of the computing profession the relevance of the *Journal* to their work. The chosen topic, which highlights these points, is:

'How the pioneering work of yesterday relates to the computing practice of today'

To be eligible a paper must deal with some aspect of this subject and must conform to the usual standards for *Journal* papers. The adjudicators will give preference to broadly based accounts, intelligible to the ordinary computer user in business or industry, tracing some specific concept or concepts from origin to practical application, with references, and commenting on the significance in relation to present computing practice.

All submissions should be sent to the Editor-in-chief to arrive no later than 28 February 1973. Authors need not be members of The British Computer Society. The result of the competition will be announced in the May 1973 issue of the *Journal* and the prize paper, together with all other entries which reach a high standard, will be published in August 1973.