

A network display program

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This paper gives an account of the development and use of software to manipulate and display networks. The work was done as part of the LSE LEGOL Project in Information Systems Analysis and Design, but the programs were written to be generally applicable; so that they might be equally suitable for displaying the results of statistical processes like single-linkage cluster analysis and path analysis, or producing structure diagrams for program or system components.

(Received April 1977)

The idea of treating a large system with many interrelated parts as a directed graph is common to many applications (See Busacker and Saaty, 1965). In particular, another LSE research project has produced software to perform well defined algorithms (e.g. partitioning into subgraphs, forming lists of successors and predecessors) on large precedence networks representing complex information systems (Waters, 1976). The original aim in the case of the present work was to find a method for displaying a network automatically, and for tracing particular paths through it in a selective way. This proved possible, using an interactive graphics terminal and a program which allowed a network of nodes and connections to be built up progressively on a screen, under user control. In the last year, facilities for partitioning, merging and reducing networks have also been included.

The first section of this paper discusses networks in the context of the LEGOL project with the help of examples; the second section outlines the capabilities of the programs developed so far.

1. The use of networks within the LEGOL project

LEGOL is intended as a formalism for describing the rules which define an information system. It has been developed mainly as the result of the study of those complex but well defined systems specified by Acts of Parliament or other legislation. The aims of the LEGOL project as a whole are described fully in Stamper (1977) and elsewhere. For the present, it is sufficient to make the point that the formalism consists of two kinds of 'rules'. What are called first-order rules are those which make some particular prescription, for example:

Section 1. 'Subject to the provisions of this Act, there shall be paid by the Minister for every family which includes two or more children, and for the benefit of the family as a whole, an allowance in respect of each child in the family other than the elder or eldest at the rate of eight shillings a week in respect of the first child other than the elder or eldest and ten shillings a week in respect of each other such child.'†

Second-order rules act upon first-order rules by specifying their dependence upon and influence over one another; they are the counterpart of such phrases as:

'Subject to the provisions of Section 7 of this Act . . .'

'Without prejudice to the provisions of paragraph 1 of Schedule 7 to the Insurance Act . . .'

Within any piece of legislation there is a complex web of inter-

relationships, both explicit and implicit, for which the idea of a precedence network appears to be appropriate. The Family Allowances Act of 1965 has been examined from this point of view. It is a short, comparatively self-contained Act, but one which implies the necessity for an administrative system to carry out its provisions. Below are some general observations about the problems involved in setting up a precedence network based upon this Act.

1. Precedence

The first question to be discussed is what exactly is meant by the word 'precedence' in this context. One of the purposes of the LEGOL formalism is to translate, with the least possible distortion, the 'static', descriptive form of an Act, stating which rules apply in which circumstances, into a more procedural language, which expresses itself in terms of operations to be performed in a certain order. But this ordering must be based upon the underlying relationships of dependence to be found in the original prose version. At the textual level, the relationships may be expressed in many different ways, as the following examples show:

Section 24. 'Notwithstanding anything in the Government of Ireland Act, 1920, the Parliament of Northern Ireland shall have power . . .'

The Family Allowances Act overrides the Government of Ireland Act in this instance.

Section 11(6). 'Where a person is entitled in respect of a child to a guardian's allowance under Section 29 of the Insurance Act . . .'

The Insurance Act provides some of the information required to administer the Family Allowances Act correctly.

Section 10(3). 'In the application of this Section to Scotland—for the reference in Subsection (1) to the bankruptcy of a person there shall be substituted a reference to the sequestration of the estate . . .'

Section 10(3) conditionally modifies Section 10(1).

Section 4(1). 'Allowances for any family shall belong . . .'

Section 4(1)(b). in the case of the family of such a man as is mentioned in Section 3(1)(b) of this Act, to him;'

Paragraph 4(1)(b) comes into force only if the conditions set out in paragraph 3(1)(b) apply.

†This extract, and all subsequent statutory quotations, are taken from the Family Allowances Act, 1965.

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Many other variants could be illustrated, in which one section of text affects the interpretation of another, by widening or narrowing its scope of application, and placing it precisely in relation to the rest of the Act, and to other relevant Acts. What the above examples have in common is that the contents of the logical 'predecessor' must be taken into account before its 'successor' can be applied correctly. At the level of the LEGOL formalism, precedence relationships will determine the sequence in which the operations specified by first-order rules must be performed. In general this will not be a simple linear sequence but a partial ordering; some parallel processing may be implied. On the other hand, some sequencing rules will be conditional or based upon criteria not always applicable. So, in order to simulate the effect of the Act in any particular circumstances, it will be necessary to trace a path selectively through first-order rules according to those precedence relationships which are actually relevant. The software described in Section 2 is intended to allow the selective 'exploration' of a network by a user, as an aid to the analysis of problems of this kind.

2. Network components: nodes

An Act of Parliament in prose form is split into parts and schedules, further divided into sections and subsections, which in turn may be subdivided into smaller units when separate cases or conditions are itemised. Textual units at any of these levels may be treated as nodes in a network. There are some difficulties about this, as the discussion below indicates; nevertheless, textual units appear to be the only objective framework within which to examine precedence relationships initially. Each node can be identified uniquely by a key which may specify:

1. Act
2. Year
3. Part or Schedule number
4. Section number
5. Subsection number
6. Item letter (a, b, c, etc.)
7. Item number (i, ii, iii, etc.)

However, the textual units making up an Act of Parliament differ greatly in function. A first attempt to categorise them led to the following six types:

2.1 Defining

These items put a precise meaning on some of the words and phrases used in the Act.

Section 2(1). 'A person shall be treated for the purposes of this Act as a child—

Section 2(1)(a). during any period whilst he is under the upper limit of the compulsory school age . . .'

2.2 Prescriptive

These items state what is to be done, who is to do it, when, where, etc.:

Section 4(2). 'Sums to be paid on account of an allowance for the family of a man and his wife living together shall be receivable either by the man or by the wife.'

Examples of the above types may contain references to other parts of the text, but they have some substantive content of their own. The remainder are more bound to the internal structure of the text.

2.3 Modifiers

These items specify changes (usually conditional) to be made in another part of the Act:

Section 14(5). 'In its application to Scotland this Section shall have effect as if—

Section 14(5)(a). in Subsection (2) the word "summary" were omitted.'

2.4 Links

These items point to some other part of the Act and state in what circumstances it is applicable:

Section 3(3). 'The provisions of the Schedule to this Act shall have effect as to the circumstances in which a man and his wife living together . . . is (sic) to be treated as maintaining a child . . .'

2.5 External References

Most Acts will make numerous references to other Acts, in whole or in part (see first two examples in paragraph 1) and these references should also be treated as separate nodes in the network, although sharply distinguished from the pieces of text to which they refer, which could be of any of the other five types.

2.6 Empty

These items have no text associated with them but are merely 'place markers' within a hierarchy. Section 3 of the Family Allowances Act has no content which is not part of Subsections 3(1), 3(2), etc. but it may be referred to as a whole from other parts of the Act, and so requires to be separately identified.

Clearly, there are difficulties in attempting to set up a network in which such disparate elements are treated on equal terms. At the level of the LEGOL formalism some nodes will eventually produce first-order rules, some second-order rules, some both or neither. Compared with orthodox programming languages, for instance, legal prose mixes together the functions of data definition, text editing, specifying procedures, transmitting arguments, etc. in a very free way. Moreover, as we have already seen, an Act is hierarchical in its structure of sections, subsections and so on, but precedence relationships may operate between nodes at any level. It does not seem to be feasible to represent both hierarchical and precedence relationships simultaneously in visual form, but it is necessary to be aware, when examining a single-level network, that a connection to, say, Section 3, implies a connection to all its constituent parts.

3. Network components: connections

A connection between two nodes implies some sort of precedence relationship between them. How can we derive these relationships from an examination of an Act? This section discusses some possible criteria.

3.1 Sequential

In a trivial sense one paragraph is the 'predecessor' of another if it comes before it in the text. However, legal prose probably relies less on the cumulative effect of a sequential scan than prose of any other kind, and textual ordering is a poor indicator of the order in which operations must be performed to carry out the provisions of an Act correctly. The Act under discussion begins by enunciating a general principle (see the quotation above) and then proceeds to further levels of detail. To apply it to any particular cases, the detailed provisions would need to be considered before deciding whether the general principle was applicable. In this particular example, various definitions of the meanings of words and phrases used throughout the Act are placed near the end, in Sections 17-19. In a 'procedural' interpretation, such definitions would have to be taken into account first. In saying that textual precedence

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assigned to the composite nodes and all key information is discarded.

With both methods, the user is asked for a composite type code to be assigned to the newly created nodes. Specific connection labels are not retained in the newly created network. The program performs a logical 'or' between the rows and columns of the connection matrix corresponding to the nodes combined, and thus several differently labelled connections may be reduced to one. Fig. 5 shows a network based on cross references as in Fig. 1, but now simplified by combining together all nodes within the same section of the Act.

1.4 Merge networks

Two networks based upon the same node set but with different connections may be merged together. If the node sets are not identical, the user is asked whether they should be combined by intersection or union. Intersection or union is performed in relation to node keys, not labels; if the two node sets happen to be labelled differently, the labels retained in the merged network are those for the second network specified to the program by the user.

Once again, specific connection labels are discarded in the resultant network, since the merge is performed by a logical 'or' of corresponding rows of the two connection matrices. However, there is a way of retaining this information, if required. As a by-product of union or intersection, the program produces two compatible networks based on the new node set but the old connection matrices and labels. The user has the option of keeping these intermediate products as well as the merged result, and since they are compatible, they can be used together by the network display program.

Fig. 6 shows a partial diagram produced in this way. It is the result of merging two networks already illustrated, (Figs. 3 and 5). In this example, connections are labelled according to their origin. Arcs labelled 'SS' represent logical connections and those labelled 'R4' represent cross references. A label 'xx' indicates that the connection was common to both original networks.

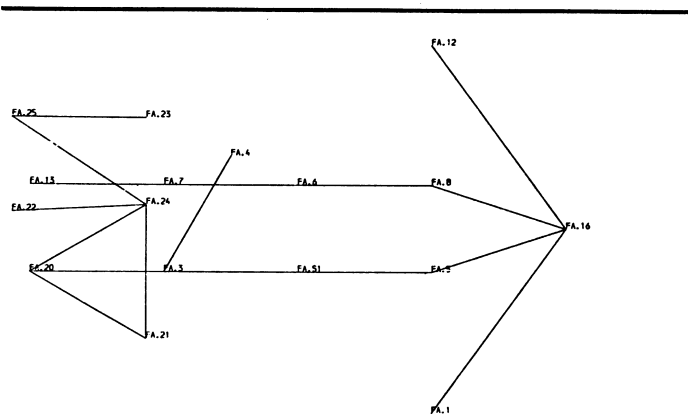


Fig. 5 Family Allowances Act, 1965 network of cross references at section level

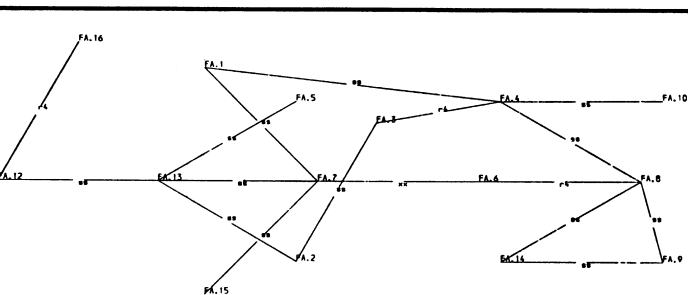


Fig. 6 Family Allowances Act, 1965 partial display of merged networks

2. The network display program

This program outputs network diagrams on to a Tektronix screen, under interactive user control. The kind of options available are indicated briefly below.

2.1 Choice of network(s)

The network to be displayed is selected by name. Two or more networks may be combined into a single display, provided their node sets are compatible (see paragraph 2.1.4). The user may terminate the display of one network and start another, during the same program execution.

2.2 Choice of starting node and its position

Any node in the network can be selected as a starting point. By convention, a node's successors are displayed to the right of that node, and its predecessors to the left. Depending upon whether the search is to go forward or backward through the network, or in both directions, the starting node may be placed on the left, the right, or the centre of the screen. Choice of successors, predecessors or all connections can be made for each subsequent node. (Occasionally the relative positions of nodes in the screen will not correctly reflect their precedence relationship. When this happens, the connection between the nodes is drawn as a broken line.) There are examples in Figs. 2 and 3.

2.3 Mode of operation

If 'automatic' mode is selected, the program will attempt to draw the connected graph containing the first node, halting only when all nodes and connections have been displayed or the diagram reaches the edge of the screen. This method is adequate where a subgraph contains only a few nodes. For more complex networks, the user may build up the diagram selectively, step by step, indicating the next part to be extended by 'pointing' with a cross-hair cursor.

2.4 Shape and size of display

There are two algorithms to select screen positions for the successors or predecessors of a given node. One method calculates a fixed distance between connected nodes, the other uses a fixed increment on the *x* axis only. Each method has its own advantages, and which is more suitable for any diagram can only be decided by trial and error. By default, the fixed distance used is two inches, on a screen 10 inches by 15. The user has the opportunity of altering this default and so drawing the diagram on a larger or smaller scale.

2.5 Connection labels

The nodes of a network are always labelled when a diagram is displayed. The arcs connecting nodes may also be labelled if necessary. Specific connection labels will be used if they were recorded when the network was set up, otherwise the network name will be output as a label when this option is requested.

2.6 Relocating the diagram

If a new node or connection to be added to a diagram will not fit on to the screen, the program will print an informative message. The user may either clear the screen and begin again with a new starting point, or redraw the existing diagram in a different position. The cross-hair cursor is used to indicate the extent and direction of the movement. Relocation may cause some nodes in the network to be 'pushed off' the screen. However, the program will remember them and their relative positions so that they will reappear if the diagram is moved back to its original place. Thus it is possible to examine, in parts, a network which is too large to go on the screen as a whole.

The layout of a diagram appearing on the screen can be stored on a stack (a sequential disc file) and retrieved later. So a user

building up a network by a series of steps can record his current state, or return to a previous state. The information saved in this way can also be filed, and used to produce microfilm copies of the screen image.

3. Applications

The work described in this paper can be considered in two ways. A piece of self-contained software has been produced, intended for use by researchers in any discipline who have networks which they wish to display and explore. It has been used, for instance, to represent patterns of co-occurrence between words in natural language texts (Jones, 1976) and, by contrast, to illustrate social interactions within a small group of people. Whatever the application, the user has the task of identifying the individual elements to be associated and what the connections between them represent. The programs can provide useful manipulations of this data.

However, from the point of view of the LEGOL project, the software is just an aid to the process of examining legal rules in terms of networks. Section 1 discussed the problems of analysing an Act of Parliament into textual elements and connections but such an analysis is only a first step. The textual units must be translated into automatically interpretable rules

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Book reviews

An Introduction to Mathematical Modelling, by Edward A. Bender, April 1978; 256 pages. (John Wiley, £11.95)

This is an interesting book, one can learn from it how to formulate and tackle a variety of problems in environmental, biological and social sciences using elementary mathematics and statistics. These fields are different from the traditional physical sciences, where mathematics has been most successfully applied in the past; a different outlook is needed, the problems are not well structured, the solutions are often qualitative rather than quantitative, the problems are practical and do not fit the conventional standard methods. The book deals with these problems by identifying the more important features while ensuring that the ignored details do not invalidate the broad results obtained. Computer methods do not feature prominently but they are used where appropriate.

The first chapter illustrates the main features of model building by considering the problems of population growth and the number of salesmen a firm should employ. Chapter 2 uses arguments based on proportionality, scale and dimensional analysis to solve problems on cost of packaging, shape of racing boats, size of animals and pendulum period. Chapter 3 applies graphical methods to problems on the missile arms race, the number of species on an island, the theory of the firm, stability in economics and group dynamics. Chapter 4 uses optimisation methods in problems concerned with inventory control, geometry of blood vessels, fighting forest fires, bartering economics and caste formation in ants. Chapter 5 applies probability to problems in population studies, sex distribution, the psychology of choice and learning, simulation of a doctor's waiting room, sediments and river networks. Chapter 6, titled Potpourri, studies temperature control in the body of the desert lizard, election procedures, respiration and carbon dioxide elimination. Chapters 7, 8 and 9 introduce differential equations and apply them to problems in the pollution of lakes, driving hazards on road curbs, polymer

and the precedence relationships between them converted into instructions about the order in which such rules ought to be applied. The application of rules by the LEGOL 'interpreter' should cause operations to be performed on stored data representing typical cases, e.g. persons and their relationships in order to generate results, e.g. details of families satisfying the conditions specified in the Act and the amount of allowance to which they would be entitled. The relationships of dependency between the different data elements used and created by LEGOL rules may also usefully be represented as a precedence network.

In the context of the LEGOL project then; software to handle networks is intended to assist the difficult process of moving from the textual to the operational level of specification, of producing an automatically interpretable set of rules which retain the essential structure of the legislation from which they were derived. As such it is a very small part of a system which may eventually prove useful to lawyers or parliamentary draftsmen.

Acknowledgements

I should like to thank Alex King of the LSE Computer Services Unit for assistance with the graphics routines.

chains, towing a water skier, stability problems, species interaction and population size, Keynesian economics and the dynamics of car following in heavy traffic. The last chapter studies stochastic models in radioactive decay, facility location and particle size in sediments.

The mathematics used is first year college level, each chapter is supplemented by further exercises, problems and references. There is an appendix on probability and a classification by subjects of the 90-odd problems considered in the book. It would be a pity if, as I suspect, this book does not fit easily the teaching program of mathematical specialists, but it should prove a useful source of material for teaching mathematics to non specialists.

I. M. KHABAZA (London)

Discrete Mathematics in Computer Science, by D. F. Stanat and D. F. McAllister, 1977; 401 pages. (Prentice-Hall, £12.80)

This book is an attempt to gather together the parts of mathematics that are used in the various branches of computer science. It contains chapters on mathematical models, mathematical reasoning, sets, binary relations, functions, counting and algorithm analysis, infinite sets and algebras. Each chapter introduces the definitions and theorems necessary for discussing the particular topic and where possible attempts have been made to provide solutions to related computing problems using an ALGOL-like programming language. There are a large number of mathematical problems set throughout the text as well as some problems that require the reader to produce solutions to programming problems.

Many students of computer science who are required to do courses on pure mathematics may well find this book will give them some indication of which parts of mathematics are useful tools in their computing studies.

M. FLOWER (Bristol)