

"Nuclear reactor calculations with the group diffusion equations on digital computers." Doctoral dissertation, Technische Hogeschool, Delft.

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## Correspondence

### An impossible program

To the Editor,  
*The Computer Journal*.

Dear Sir,

Strachey's letter\* under this title gave rise to some discussion among my colleagues, some of it along the lines of ApSimon's letter,† and it recalled to me similar discussions in my school-days about the validity of *reductio ad absurdum* proofs in geometry. If ApSimon's objections were valid, they would apply to all proofs of this sort, and invalidate a fair part of the structure of mathematics from Euclid onward.

Much more interesting to me is a corollary which I have not seen stated elsewhere. Consider the following program:

```
begin integer a, b, c, m;
  for m := 3, m + 1 while true do
    for a := 1 step 1 until m do
      begin for b := 1 step 1 until a do
        for c := a step 1 until a + b do
          if  $a^m + b^m = c^m$  then go to out;
        if  $a > 2$  then begin
          for b := 1 step 1 until m do
            for c := m step 1 until m + b do
              if  $m^a + b^a = c^a$  then go to out end
            if a
          end for a and for m;
        out: end program
```

This, if I have not made any errors in writing it, is a rather inefficient search program for a counter-example to Fermat's last theorem, covering all possible cases in a single denumerable infinity (this is important). Application of the function  $T$  to this program would constitute a proof or a refutation of this theorem. (The inefficiency of the program is irrelevant for this purpose; one might well imagine that simplicity would be more helpful.) A similar technique would apply

\* This *Journal*, January 1965, p. 313.

† *Ibid.*, April 1965, p. 72.

immediately to a great number of unproved conjectures in number theory. Alas, that it cannot be done in this way!

Yours sincerely,  
BRYAN HIGMAN.

Windy Sayles,  
Felden,  
Hemel Hempstead.  
7 May 1965.

To the Editor,  
*The Computer Journal*.

Dear Sir,

We wish to bring to the notice of your correspondent, Mr. ApSimon ("An impossible program", this *Journal*, April 1965, p. 72), the method of proof by *reductio ad absurdum*, in which a hypothesis is proved false by assuming its truth and deriving a contradiction. In this instance, the hypothesis is:

- (i) There is (i.e., it is possible to write) a Boolean function with a routine as argument whose value is **true** if the routine terminates and **false** if it does not.

Call such a function  $T[R]$ .

From (i) it follows, as in Strachey's letter (this *Journal*, January, 1965, p. 313):

- (ii) There is a routine  $P$  which terminates if  $T[P] = \text{false}$ , and fails to if  $T[P] = \text{true}$ .

This is a contradiction. Hence the hypothesis (i) is false, which was to be proved.

Yours faithfully,  
W. F. LUNNON,  
C. F. J. OUTRED.

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The University,  
Manchester 13.  
26 May 1965.

[Correspondence contd. on next page]